CONTROL FLOW GRAPHS

 Motivation: language-independent and machineindependent representation of control flow in programs used in high-level and low-level code optimizers. The flow graph data structure lends itself to use of several important algorithms from graph theory.

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Basic Blocks A straight line sequence of code a maximal sequence of instructions that can be entered only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of only at the first of them and exited only from the last of the first of the first of them and exited only from the last of the first of them and exited only from the last of the first of the first of them and exited only from the last of the first of the first of them and exited only from the last of the first of the first of the first of them and exited only from the last of the first of the first of them and exited only first of the first of them and exited only first of the first of t

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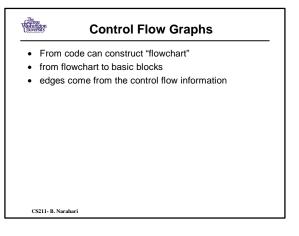
Control Flow Graph: Definition
 A control flow graph CFG = (N_c; E_c; T_c) consists of
 N_c, a set of nodes. A node represents a straight-line sequence of operations with no intervening control flow i.e. a basic block.

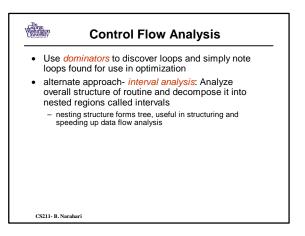
- $E_c I N_c \times N_c \times Labels$, a set of labeled edges.
- T_c, a node type mapping. T_c(n) identies the type of node n as one of: START, STOP, OTHER.

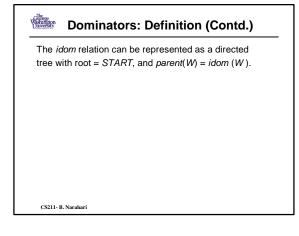
We assume that *CFG* contains a unique *START* node and a unique *STOP* node, and that for any node *N* in *CFG*, there exist directed paths from *START* to *N* and from *N* to *STOP*.

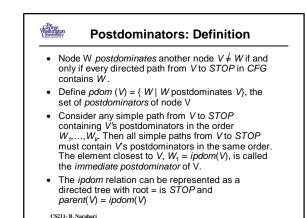
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Dominators: Definition Node V dominates another node $W \neq V$ of and only if every directed path from *START* to W in *CFG* contains V. Define *dom* (W) = { V | V dominates W }, the set of dominators of node W. Consider any simple path from *START* to W containing W 's dominators in the order V_1, \dots, V_k . Then all simple paths from *START* to W must contain W 's dominators in the same order. The element closest to W, $V_k = idom$ (W), is called the *immediate* dominator of W.

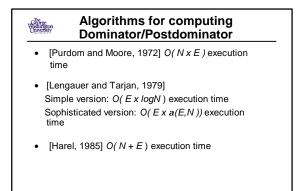








Example: Dominator and Postdominator Trees



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Loop Nesting Structure of a Control Flow Graph

- The loop nesting structure of a CFG is revealed by its *interval structure:*
- Edge e = (x, h, l) in CFG is called a *back edge* if h 1 dom (x); h is called a *header* node, and x is called a *latch node*.
- The strongly connected region defined by back edge e = (x, h, l) is STR(e), which consists of the nodes and edges belonging to all paths from node h to node x, along with the back edge (x,h, l).
- The *interval with header h, l(h),* is defined as the union of *STR*(*e*) over all back edges e targeted to header node *h*.

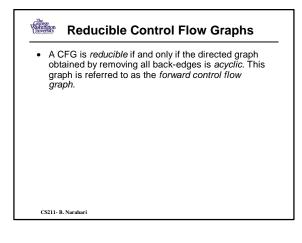
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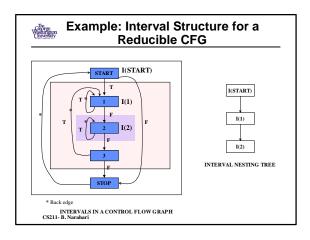
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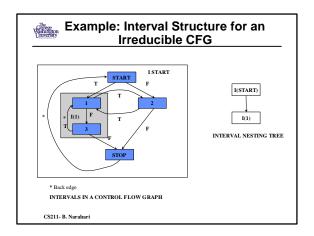
Loop Nesting Structure of a Control Flow Graph (Contd.) Interval nesting is defined by the subgraph relationship. I(h₁) is a subinterval of I(h₂) if I(h₁) is a subgraph of I(h₂). The interval nesting relation can then be represented by a unique interval nesting tree (or forest of trees).

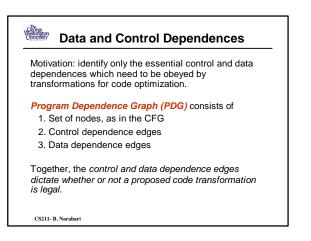
• It is convenient to add a pseudo-edge from *STOP* to *START* to make *START* a header node with *I(START)* = entire CFG, and thus force the interval relation to be a single tree rather

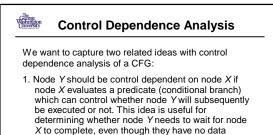
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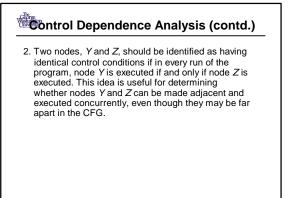






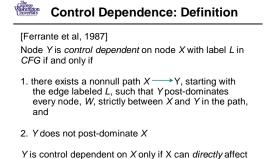
dependences.

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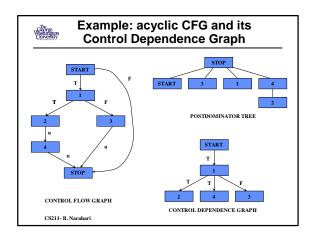


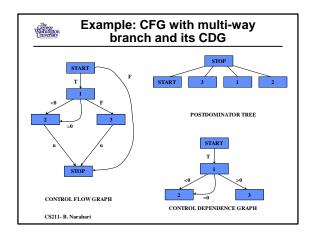
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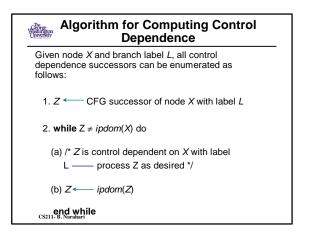
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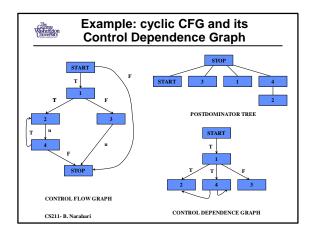


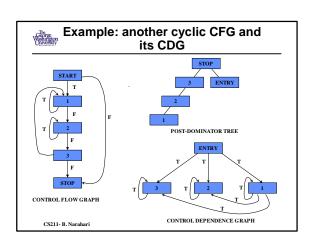
Y is control dependent on X only if X can *directly* affect whether Y is executed or not; *indirect* control dependence can be defined as the transitive closure of control dependence CS111-B. Narahari











Properties of Control Dependence

- CDG is a tree \rightarrow CFG is structured
- CDG is acyclic → CFG is acyclic
- CDG is cyclic \rightarrow CFG is cyclic

The control conditions of node Y is the set,

 $CC(Y) = \{(X,L) | Y \text{ is control dependent on } X \text{ with label } L \}$

Two nodes, *A* and *B*, are said to be *identically control* dependent if and only if they have the same set of control conditions i.e. CC(A) = CC(B)

Data Dependence Analysis

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> If two operations have potentially interfering data accesses, data dependence analysis is necessary for determining whether or not an interference actually exists. If there is no interference, it may be possible to reorder the operations or execute them concurrently.

The data accesses examined for data dependence analysis may arise from array variables, scalar variables, procedure parameters, pointer dereferences, etc. in the original source program.

Data dependence analysis is conservative, in that it may state that a data dependence exists between two statements, when actually none exists.

Data Dependence: Definition

A data dependence, $S_1 \rightarrow S_2$, exists between CFG nodes S_1 and S_2 with respect to variable X if and only if

- 1. there exists a path $P: S_1 \rightarrow S_2$ in *CFG*, with no intervening write to *X*, and
- 2. at least one of the following is true:

(a) (flow) X is written by S₁ and later read by S₂, or
(b) (anti) X is read by S₁ and later is written by S₂ or
(c) (output) X is written by S₁ and later written by S₂

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Def/Use chaining for Data Dependence Analysis

A *def-use chain* links a definition D (i.e. a write access of variable X to each use U (i.e. a read access), such that there is a path from D to U in CFG that does not redefine X.

Similarly, a *use-def chain* links a use U to a definition D, and a *def-def chain* links a definition D to a definition D' (with no intervening write to X in all cases).

Def-use, use-def, and def-def chains can be computed by data flow analysis, and provide a simple but conservative way of enumerating flow, anti, and output data dependences. CS11-B.Nembari

Static single assignment (SSA) form

- Static single assignment (SSA) form provides a more efficient data structure for enumerating defuse, def-use and def-def chains.
- SSA form requires that each use be reached by a single def (when representing def-use information; analogous requirements are enforced for representing use-def and def-def information). Each def is treated as a new "name" for the variable.
- Each variable is assumed to have a dummy definition at the *START* node of the CFG.

