













## How to utilize the similarities?

- Adopting human authentication protocols in lowcost pervasive computing devices.
- Allowing a person to log onto an un-trusted terminal while someone spies over his/her shoulder, without the use of any scratch paper or computational devices.
- A simple password would be immediately revealed to an eavesdropper.













## Learning Parity in the Presence of Noise

Suppose that an eavesdropper, i.e., a passive adversary, captures q rounds of the HB protocol over several authentications and wishes to impersonate Alice. Consider each challenge a as a row in a matrix A; similarly, let us view Alice's set of responses as a vector z. Given the challenge set A sent to Alice, a natural attack for the adversary is to try to find a vector x1 that is functionally close to Alice's secret x. In other words, the adversary might try to compute a x1 which, given challenge set A in the HB protocol, yields a set of responses that is close to z. (Ideally, the adversary would like to figure out x itself.)









# Defending Against Active Attacks HB+ requires the tag (playing the role of the human), to generate a random k-bit string b on each query. If the tag (or human) does not generate uniformly distributed b values, it may be possible to extract information on x or y.





# Security Proofs Notation and Definitions: define a tagauthentication system in terms of a pair of probabilistic functions (*R*, *T*), namely a reader function *R* and a tag function *T*. *T* is defined in terms of a noise parameter η, a *k*-bit secret *x*, and a set of *q* random *k*-bit vectors {*a*(*i*)}*q*(*i*=1) Let *q* be the maximum number of protocol invocations on *T* in this experiment.



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**m k1** m k, 4/9/2008















It is entirely possible that the adversary's advantage is preserved when, for each column j, samples are drawn from the RAji subspace for a matrix Aj





### Reduction of LPN to HB+-Attack

 By combining Lemmas 1 and 3, we obtain a concrete reduction of the LPN problem to the HB+-attack experiment.

◆ The theorem follows directly from Lemmas 1 and 3.
Theorem 1. Let Adv<sup>HB+-Attack</sup>(k, η, q, t<sub>1</sub>, t<sub>2</sub>) = ζ, where U is a uniform distribution over binary matrices Z<sup>g×k</sup><sub>2</sub>, and let A be an adversary that achieves this -advantage. Then there is an algorithm that can solve a random  $q' \times k$  instance of the LPN problem in time  $(t'_1, t'_2)$  with probability  $\frac{1}{k}$ , where  $t'_1 \leq k^2 Lq(2 + \log_2 q)t_1$  $t'_2 \le 2k^2Lt_2, q' \le kLq(2 + \log_2 q), and L = \frac{128k^4(\ln k - \ln \ln k)}{(1 - 2\eta)^2(\zeta^3(k - 2) + 2)^2}.$ 

To put this in asymptotic terms, the LPN problem may be solved by an adversary where  $\operatorname{Adv}^{HB^+-Attack}(k,\eta,q,t_1,t_2) = \zeta$  in time  $O(\frac{(k^5 \log k)(q \log q) t}{(1-2q^2)\zeta^6})$ where  $t = t_1 + t_2$ .

### **Conclusion and Open Questions**

- Presents a new authentication protocol named HB+ that is appropriate for low-cost pervasive computing devices.
- The HB+ protocol is secure in the presence of both passive and active adversaries.
- The HB+ should be implemented within the tight resource constraints of today's EPC-type RFID tags.
- The security of the HB+ protocol is based on the LPN problem, whose hardness over random instances remains an open question.



