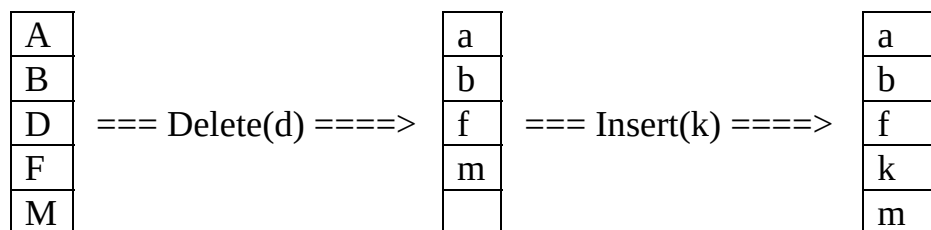


Linked Lists Structures

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1. Motivation

- Insertion & Deletion in an ordered array require moving elements up or down (left or right).
- Manipulating ordered lists of varying sizes
- Example:



- Solution:
 - use linked lists
 - creation of variable's storage space in memory during the execution (rather than compilation) of the program
 - Each data (a set of data) is associated with an address: form a node.
- Implementation:
 - Use heap
 - Allocation of variable's storage space: needs a variable that holds the address of that space.
 - Pascal: pointer variable
 - Ada: Access variable
 - C: For any type in C, there is a corresponding type pointer-to-T: The value of the pointer is an address of memory.

- Requirements:
 - Mechanism to define the structure of a node (all fields)
 - A way to create a node
 - A way to free no longer needed nodes

2. Declaration of a node

- A C++ Class:

```
class Node{

    Private:
        element_type data;
        Node *left_link;
        Node *right_link;
}
```

- Create an object node:

```
Node head_ptr;
Node tail_ptr;
```

- As a structure:

```
Struct Node {
    element_type data;
    struct Node *left_link;
    struct Node *right_link;
};
```

- Struct Node *node_pointer;

- node_pointer start, end;

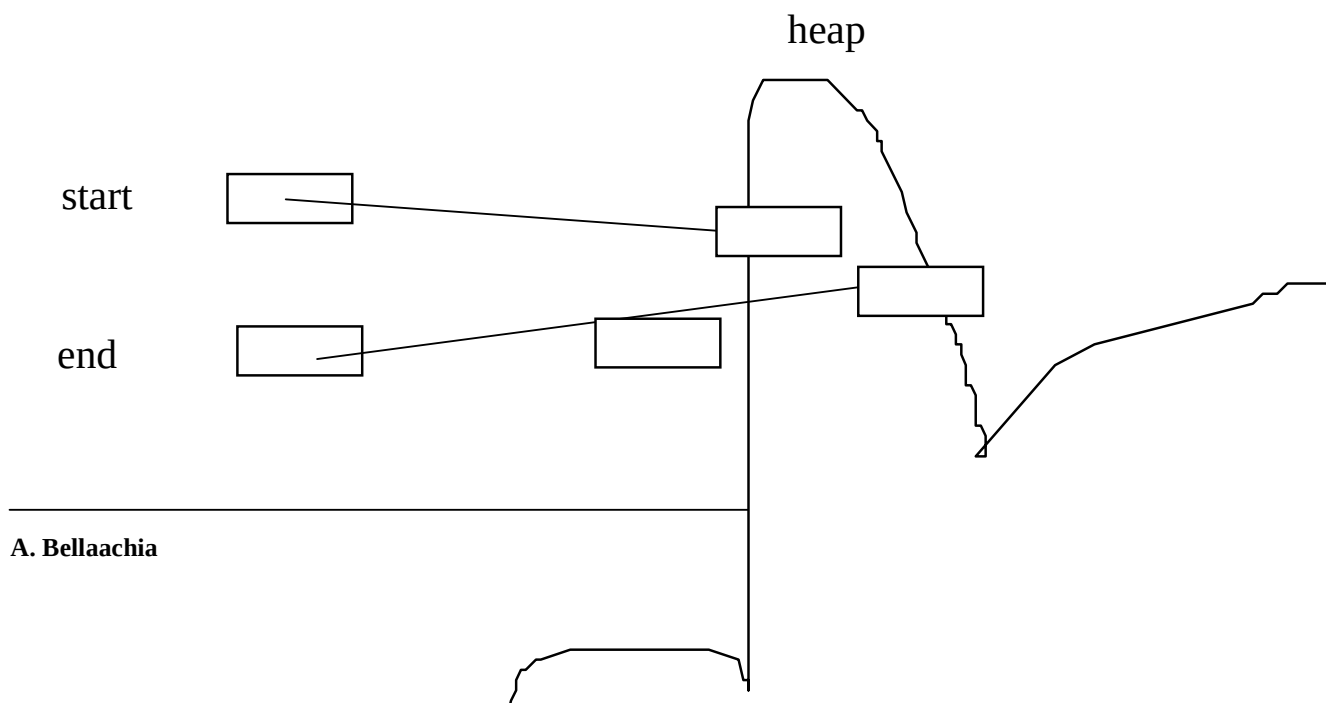
- Access Fields:

`start->data = element;`

- Constant nil:
 - the pointer does not point to any node
 - `start = nil` or `null`;

2.1. Operations on pointers

- Comparison: `start == end`, etc.
- Assignments: `start = end`, etc.
- Arithmetic: depending on the language
- Creation of a node:
 - Primitive procedure: `malloc`, `new`, etc.



2.2. Disposition of a node

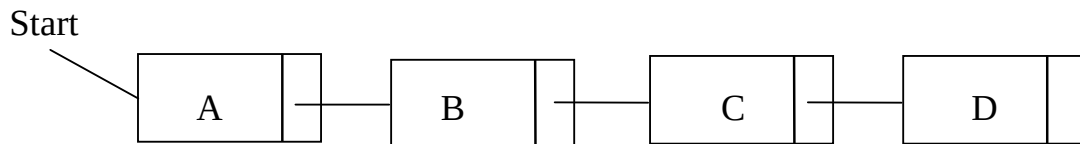
- Primitive procedure: `free(p)`, `dispose(p)`, etc.

2.3. Singly Linked Lists

- One-way linked lists
- One-way linked lists with head and tail
- Circular one-way linked lists

3. One-way linked lists

- **An example:**

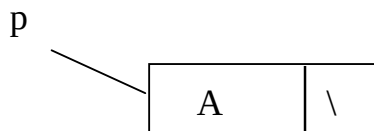


- **Operations:** Sorted or Unsorted

- Insertion
- Deletion
- Find

3.1. Insertion in an unsorted list:

- Creation of a node:



- Case 1: When the list is not empty; start != nil.

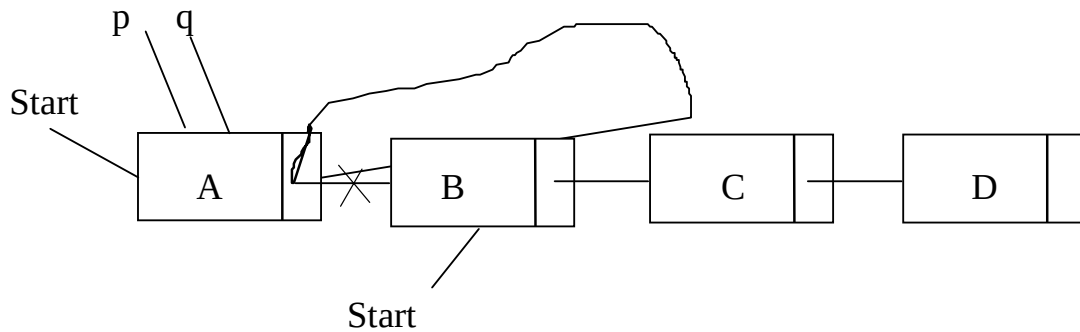
```
p->link = start;  
start = p;
```

- Case 2: When the list is empty; start=nil.

```
start = p;
```

3.2. Deletion

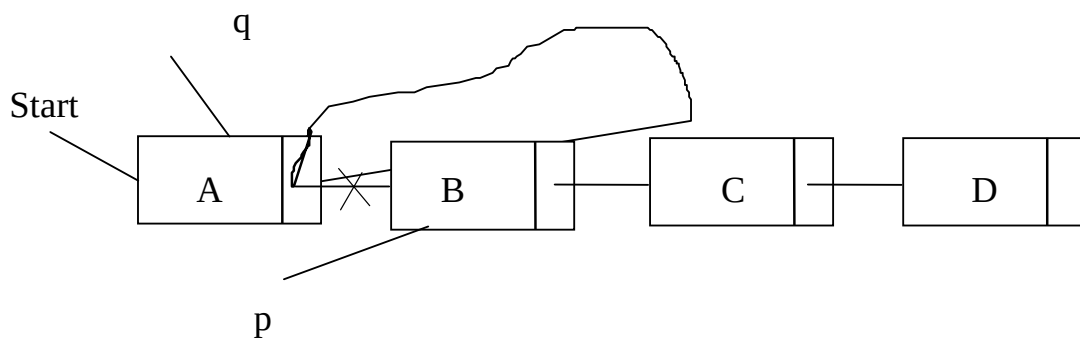
- Case 1: The first element of the list



Delete(A):

```
p = q = Start  
Start = Start->link;  
free(q);
```

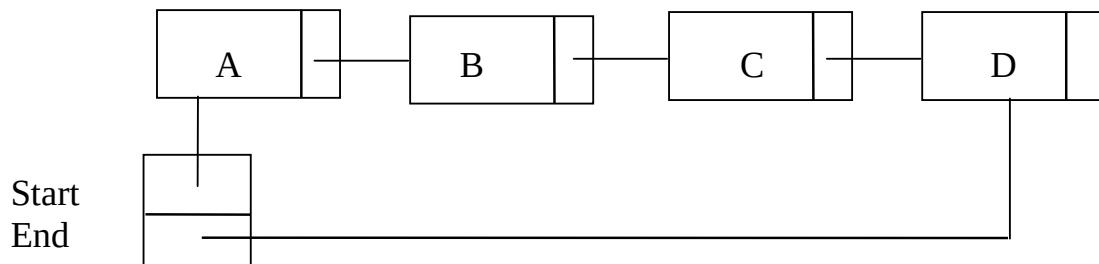
- Case 2: An element different than the first one in the list



```
q ->link = p->link;  
free(p);
```

4. One-way linked lists with Head and Tail

- An example:

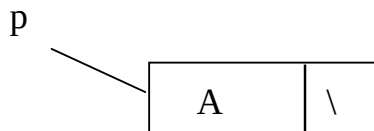


4.1. Operations: Sorted or Unsorted

- Insertion
- Deletion
- Find

4.2. Insertion in an unsorted list:

- Creation of a node:



- Case 1: When the list is not empty; start != nil and Tail != nil;

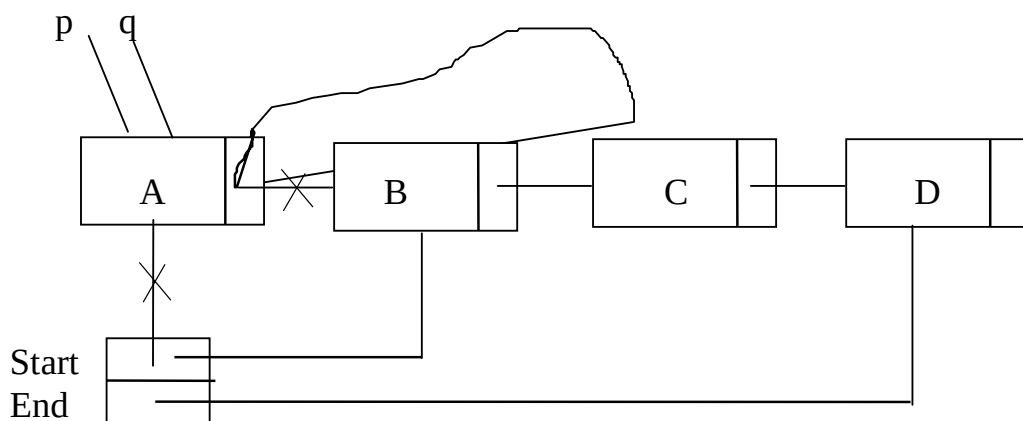
```
p->link = start;
start = p;
```

- Case 2: When the list is empty; start=nil.

```
start = p;
Tail = p;
```

4.3. Deletion

- Case 1: The first element of the list



Delete(A):

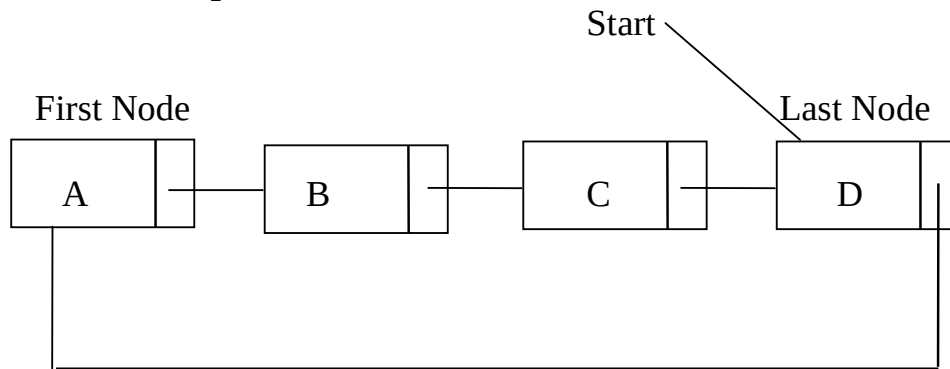
```
p = q = Start
Start = Start->link;
free(q);
```

- Case 2: An element different than the first one in the list

Same as in the case of one-way linked list.

5. Singly Circular Linked Lists

- **An example:**



5.1. Operations: Sorted or Unsorted

- Insertion
- Deletion
- Find

5.2. Insertion in an unsorted list:

- Creation of a node:

The diagram shows a pointer P pointing to a new node. The node is a rectangle divided into two parts: the data field contains 'A' and the pointer field contains a backslash '\', representing nil.

- Case 1: When the list is not empty; start $\neq$ nil;

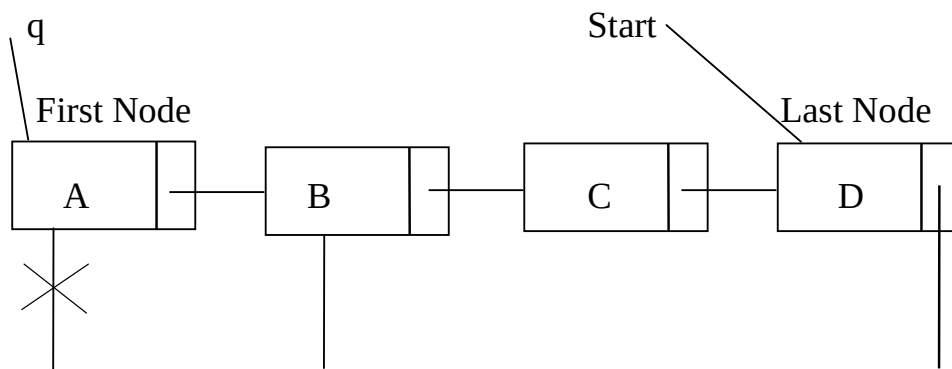
```
p->link = start;  
start->link = p;  
start = p;
```

- Case 2: When the list is empty; start = nil.

```
start = p;  
p-link = p;
```

5.3. Deletion

- Case 1: The first element of the list



Delete(A):

```
q = start->link;  
Start->link = q->link;  
free(q);
```

- Case 2: The last element of the list

Do as Homework.

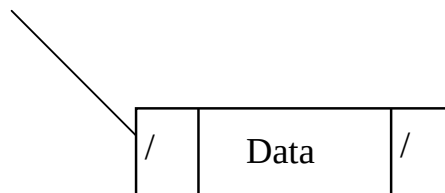
- Case 3: An element different from the first and last element of the list.

Same as in the case of one-way linked list.

6. Doubly Linked Lists

- Type of nodes: Declaration of a node:

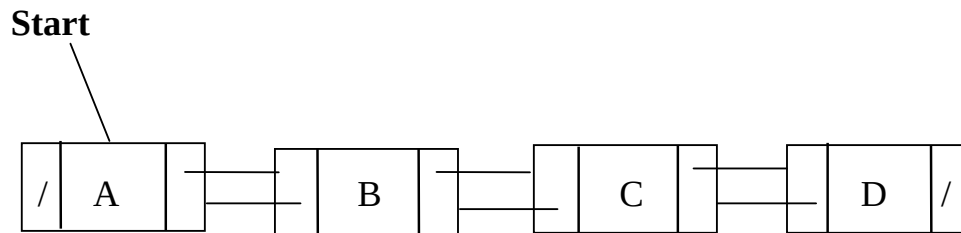
```
struct nodetype{  
    struct nodetype *Llink;  
    element_type data;  
    struct nodetype *Rlink;  
};
```



- Types:
 - Simple doubly linked lists
 - Circular doubly linked lists

7. Simple doubly linked lists

- An example



7.1. Operations: Sorted or Unsorted

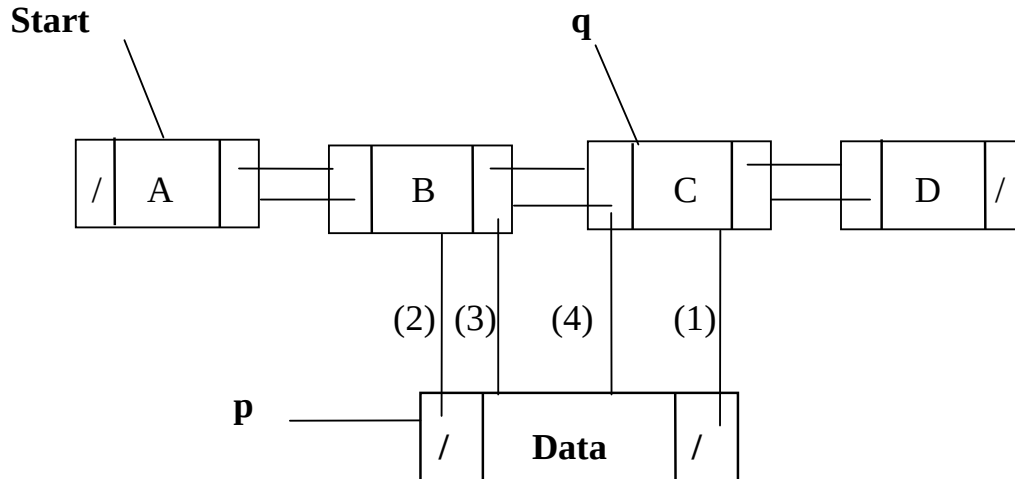
- Insertion
- Deletion
- Find

7.2. Insertion in an unsorted list:

- Creation of a node:



- Case 1: When the list is not empty; start $\neq$ nil;



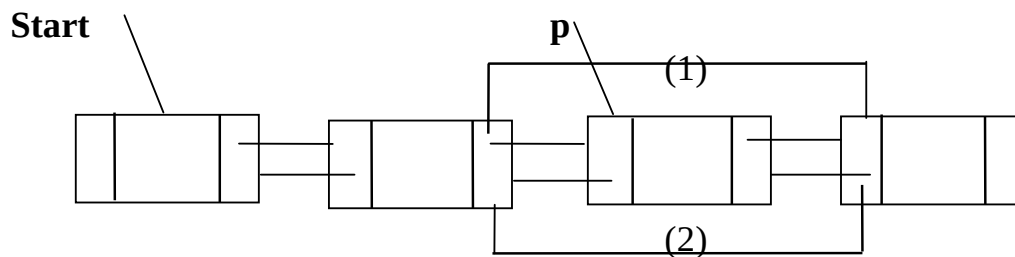
- (1) $p \rightarrow Rlink = q$;
- (2) $p \rightarrow Llink = q \rightarrow Llink$;
- (3) $q \rightarrow Llink \rightarrow Rlink = p$;
- (4) $q \rightarrow Llink = p$;

- Case 2: When the list is empty; start=nil.

start = p;

7.3. Deletion

- Case 1: An element different from the first and last element of the list.



Delete(C):

```
p->Llink->Rlink = p->Rlink;  
p->Rlink->Llink = p->Llink;  
free(q);
```

- Case 2: The first element of the list.

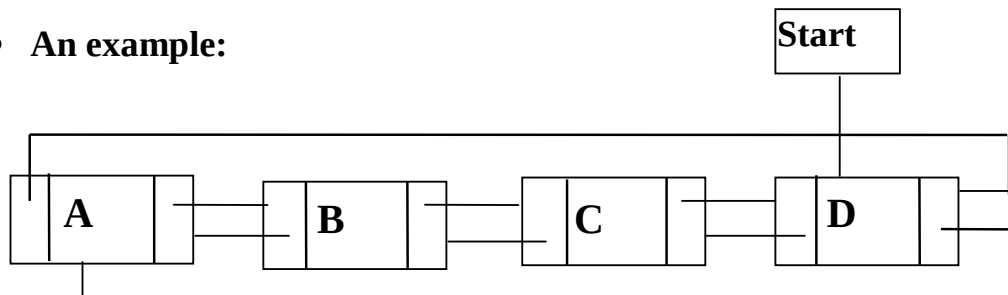
Do as Homework.

- Case 3: The last element of the list.

Do as Homework.

8. Circular doubly linked lists

- An example:



8.1. Operations: Sorted or Unsorted

- Insertion
- Deletion
- Find

8.2. Insertion in an unsorted list

- Case 1: When the list is not empty; start $\neq$ nil;
- Case 2: When the list is empty; start=nil.

8.3. Deletion

- Case 1: An element different from the first and last element of the list.
- Case 2: The first element of the list.
- Case 3: The last element of the list.