## SOLUTION QUESTION 7.15:

Julie Myers, a graduating senior in accounting, is preparing for an interview with a Big Eight accounting firm. Before the interview, she sets her chances of eventually getting an offer at $50 \%$. Then, on thinking about her friends who have interviewed and gotten offers from this firm, she realizes that of the people who have interviewed and gotten offers from this firm, 95\% had good interviews. On the other hand, of those who did not receive offers, $75 \%$ said they had good interviews. If Julie Myers has a good interview, what are her chances of receiving an offer?

SOLUTION: From the text we conclude:

$$
\operatorname{Pr}(\text { Offer })=0.50,
$$

$\operatorname{Pr}($ Good Interview $\mid$ Offer $)=0.95, \operatorname{Pr}($ Good Interview $\mid$ No Offer $)=0.75$

We want to know: $\operatorname{Pr}($ Offer| Good Interview). The solution uses Bayes Theorem. We will split the solution in two steps by first calculating $\operatorname{Pr}(G o o d$ Interview) by using the Law of Total Probability and second use the calculation rule for conditional probabilities to calculate $\operatorname{Pr}(\mathrm{Offer} \mid \mathrm{Good}$ Interview).

## STEP 1: Apply Law of Total Probability

## $\operatorname{Pr}($ Good Interview $)=\operatorname{Pr}($ Good Interview $\mid$ Offer $) \operatorname{Pr}($ Offer $)+$ $\operatorname{Pr}($ Good Interview | No Offer) $\operatorname{Pr}($ No Offer $)$

Hence

$$
\operatorname{Pr}(\text { Good Interview })=0.95 \cdot 0.50+0.75 \cdot 0.50=0.85
$$

## STEP 2: Apply calculation rule for conditional probability

$\operatorname{Pr}($ Offer $\mid$ Good Interview $)=\frac{\operatorname{Pr}(\text { Good Interview } \mid \text { Offer }) \operatorname{Pr}(\text { Offer })}{\operatorname{Pr}(\text { Good Interview })}$
Hence,

$$
\operatorname{Pr}(\text { Offer } \mid \text { Good Interview })=\frac{0.95 \cdot 0.50}{0.85}=0.559
$$

Conclusion: Only a slight increase is observed in our beliefs in getting an offer after we had a good job interview (from 0.500 to 0.559 ). The reason is that the people's judgement regarding "Good Interviews" is not very informative. Indeed,
$\operatorname{Pr}($ Good Interview $\mid$ Offer $)=0.95, \operatorname{Pr}($ Good Interview $\mid$ No Offer $)=0.75$.

