

LECTURE NOTES: EMGT 234

SOURCE:

Polat Gulkan, Mustafa Erdik, 1988. "Probabilistic Tools in Earthquake Hazard Forecast: A Case Study for Turkey",
Seismic Hazard in Mediterranean Regions,
229-253.

Question 1: How often do Earth Quakes Occur?

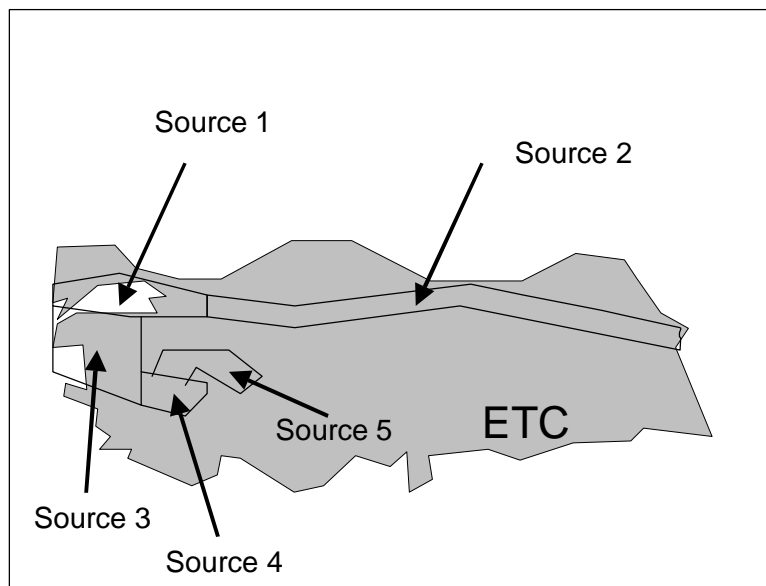
The Region in question has a finite number of sources that could produce measurable earthquakes: $j=1, \dots, N$

Definition:

An Earthquake is measurable when its intensity falls between intensity levels $[i_{min}, i_{max}]$

A single source generates Earth Quakes following the Poissonian Law:

- Let ν_j be the annual rate of number of earthquakes from source j .



- Let $[0, t]$ be a time period under consideration. For example, the next 10 years.

- Let $N_j(t)$ be the total number of earth quakes from Source j in the period $[0, t]$.

$$Pr(N_j(t) = n) = \frac{(\nu_j t)^n}{n!} e^{-(\nu_j t)}$$

- Let T_j the time between two consecutive earthquakes from source j

$$Pr(T_j > t) = 1 - e^{-(\nu_j t)}$$

Question 2: Given that an Earth Quake occurs what is the likelihood of its intensity level

Assessing Conditional Probability Distribution for Intensity Levels in from a particular source

Assumption:

Intensity level of interest ranges from $[i_{min}, i_{max}]$

For example:

$$i_{min} = 2.0 \text{ on Richter Scale}$$

Notation: EQ = Earthquake

Definition:

$n(i)$:= the number of EQ's with intensity level more than i in a geographic region

Past studies have shown that:

$$n(i) = \exp(a + b(i - i_{min})), b < 0$$

n_{min} the number of EQ's
with intensity level more than i_{min}

n_{max} the number of EQ's
with an intensity level more than i_{max}

STEP 1:

Determine total number of EQ's of interest (those that caused some level of damage) for a particular geographic region and set this equal to n_0 . Assume that there is one Earth Quake of level higher than i_{max} . Set

$$n_{min} = n_0 + 1$$

Solve for the constant a , via

$$n_{min} = \exp(a)$$

STEP 2:

Go back into your historical data set and determine the EQ with the highest intensity level. Set i_{max} equal to this intensity level. Assumption, $n_{max} = 1$.

Solve for the constant b , via

$$n_{max} = \exp(a) \exp(i_{max} - i_{min}), b < 0$$

$$1 = n_{min} \exp(b (i_{max} - i_{min}))$$

$$\Rightarrow b = \frac{\ln \frac{1}{n_{min}}}{i_{max} - i_{min}}$$

Note:

- **Constant α** depends on the length of the time period over which Earth Quakes have been recorded and the number of Earth Quakes recorded in this period.

- **Constant b** depends on the maximum intensity level observed over the time period and the lowest intensity level of interest.

STEP 3:

$$Pr(EQ \text{ of intensity } [i_{min}, i_{max}) = \frac{n_{min}-1}{n_{min}}$$

STEP 4:

$$Pr(EQ \text{ of intensity } [i_{min}, i) = \frac{n_{min} - n(i)}{n_{min}}$$

STEP 5:

$$Pr(EQ\ of\ intensity\ [i_{low}, i\ |EQ\ of\ intensity\ [i_{min}, i_{max}\])$$

$$\frac{Pr(EQ\ of\ intensity\ [i_{low}, i\])}{Pr(EQ\ of\ intensity\ [i_{min}, i_{max}\])$$

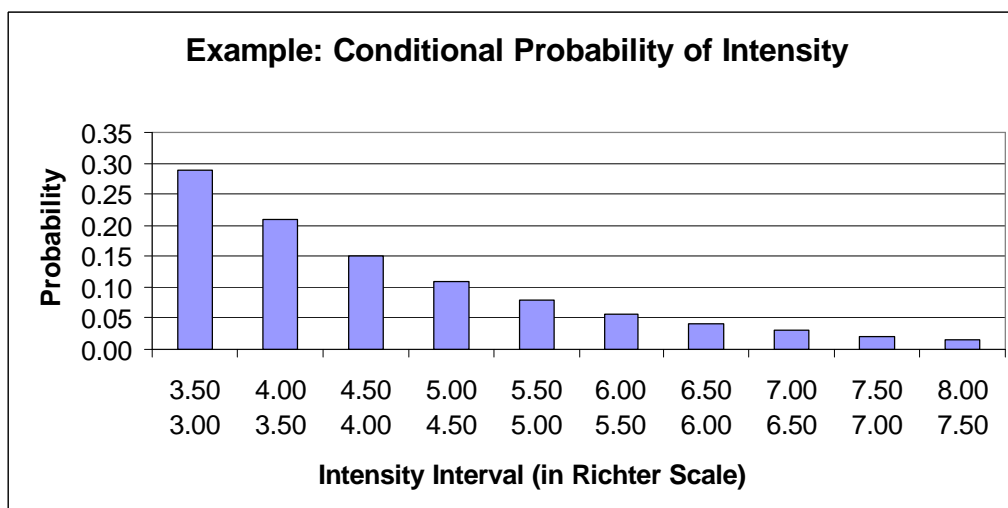
$$\frac{n_{min} - n(i)}{n_{min}} \quad \frac{n_{min}}{n_{min} - 1} \quad \frac{n_{min} - n(i)}{n_{min} - 1}$$

or using

$$n = exp(a + b(i - i_{min}))$$

$$Pr(EQ\ of\ intensity\ i_{low}, i\ |EQ\ of\ intensity\ [i_{min}, i_{max}\])$$

$$\frac{exp(a) - exp(a + b(i - i_{min}))}{exp(a) - 1}$$



Question 3: Given that an Earth Quake occurs at a source with intensity i what is the intensity at a certain site a particular distance away from the source

Let:

i_s : *Intensity at the site*

i : *Intensity at the source*

R : *Distance away from the source.*

$$i_s = i - w(R) + \epsilon$$

where

$w(R)$: *Some function of R*

ϵ : *Some random error term*